



HELLENIC OPEN UNIVERSITY

# Advanced Quantitative Methods for Managers

**VOLUME 1**

M. G. KAVUSSANOS

## Advanced Quantitative Analysis



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# ADVANCED QUANTITATIVE METHODS FOR MANAGERS

## Advanced Quantitative Analysis

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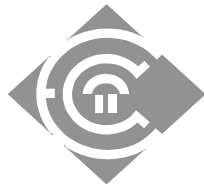
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HELLENIC OPEN UNIVERSITY

SCHOOL OF SOCIAL SCIENCES

PROGRAM OF STUDIES

**Masters in Business Administration**

MODULE

**Advanced Quantitative Methods For Managers**

VOLUME 1

**ADVANCED QUANTITATIVE ANALYSIS**

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